Tutorial: Statistical Analysis of Optimization Algorithms with R

Statistical Analysis of Optimization Algorithms with R

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July 2012

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ACM 978-1-4503-1178-6/12/07.

Tutorial: Statistical Analysis of Optimization Algorithms with R

Your Instructors Today

- ▶ Dr. Thomas Bartz-Beielstein is a professor for Applied Mathematics at Cologne University of Applied Sciences. He has published more than several dozen research papers, presented tutorials about tuning, and has edited several books in the field of Computational Intelligence.
- Mike Preuss is research associate at the Computer Science Department, TU Dortmund. His main fields of activity are EAs for real-valued problems and their application in numerous engineering domains
- Martin Zaefferer is a research assistant at Cologne University of Applied Sciences. His research interests include computational intelligence, applications of knowledge discovery and sequential parameter optimization.

Agenda

Introduction

R Basics and Technical Details

Exploratory Data Analysis

Distributions and Random Number Generation

Design of Experiments (DoE)

R-based automated analysis and tuning, e.g., sequential parameter optimization

Reporting results. Automated report generation using Sweave

R-based optimization and benchmarking resources

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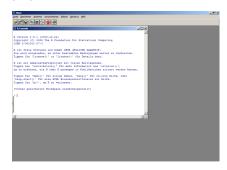
Goals

- ► Most effective approach for learning how to design, conduct, and analyze experiments that optimize performance in algorithms
- ▶ Show how to use statistically designed experiments to
 - Obtain information for characterization and optimization of algorithms
 - Improve their performance
 - Design and develop new operators and algorithms
- ► Learn how to evaluate algorithm alternatives, improve their field performance and reliability
- Conduct experiments effectively and efficiently
- ► Hands-on tutorial which
 - demonstrates how to analyze results from real experimental studies, e.g., experimental studies in EC
 - ▶ gives a comprehensive introduction in the R language
 - introduces the powerful GUI "rstudio" (http://rstudio.org)
 - will be held in an interactive manner, i.e., the analyses will be performed in real time.

−R Basics and Technical Details

Linterfacing with R

Pure R



 Windows version comes with a simple build-in GUI

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R Basics and Technical Details Iris Data

The Famous Iris Data Set

- ► Four features were measured from each sample
- ▶ Length and width of sepal and petal, respectively

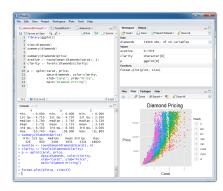


Photo by[7]

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R Basics and Technical Details
Interfacing with R

RStudio



- ► Powerful productivity tools
 - Syntax highlighting, code completion, and smart indentation
 - ► Execute R code directly from the source editor
 - Easily manage multiple working directories using projects
 - Quickly navigate code using typeahead search and go to definition

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R Basics and Technical Details

The Famous Iris Data Set: Iris Setosa, Virginica, and Versicolor

- ▶ Based on the combination of the four features, Fisher [5] developed a linear discriminant model to determine which species from these four measurements
- ▶ Used as a typical test for many other classification techniques







▶ Iris setosa [3], iris virginica [10], and iris versicolor [8]

∟_{Iris Data}

The Famous Iris Data Set: Hands-on Exercises

- ▶ How to generate a scatter plot of Fisher's Iris data with pure R code
- First, we load the data frame:
- > data(iris)
 - ► Next, we have a quick look at the data (here, only the first three rows are shown)
- > iris[1:3,]

	Sepal.Length	Sepal.Width	Petal.Length	${\tt Petal.Width}$	Species
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa

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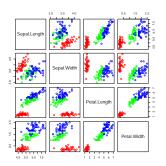
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The Famous Iris Data Set: Hands-on Exercises

- ▶ Finally, a scatter plot is generated with the pairs() function.
- > pairs(iris[,1:4], col=c("red", "green", "blue")[as.numeric(iris\$Species)])



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The Famous Iris Data Set: Hands-on Exercises

▶ The summary() command gives a quick overview

```
> options(width=70)
```

```
> summary(iris)
```

```
Sepal.Length
                Sepal.Width
                                Petal.Length
                                                Petal.Width
Min. :4.300
               Min.
                      :2.000
                               Min.
                                     :1.000
                                               Min.
                                                    :0.100
1st Qu.:5.100
               1st Qu.:2.800
                               1st Qu.:1.600
                                               1st Qu.:0.300
Median :5.800
               Median :3.000
                               Median :4.350
                                               Median :1.300
Mean :5.843
               Mean
                      :3.057
                               Mean :3.758
                                               Mean
                                                    :1.199
3rd Qu.:6.400
               3rd Qu.:3.300
                               3rd Qu.:5.100
                                               3rd Qu.:1.800
      :7.900
                                                      :2.500
                      :4.400
                               Max.
                                      :6.900
                                               Max.
      Species
setosa
         :50
versicolor:50
virginica:50
```

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A Gentle Introduction to R.

- ▶ Some of the following examples are based on [9]
- ▶ R can be used as a calculator

> 2+2

Γ17 4

> 5*3*4

[1] 60

Data entry

```
> year <- c(1800,1850,1900,1950,2000)
> pop <- c(18,54,500,1701,7731)</pre>
```

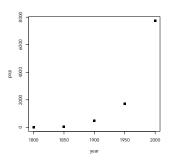
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A Simple plot

```
Data entry:
```

```
> print( c(year,pop))
[1] 1800 1850 1900 1950 2000      18      54      500 1701 7731
> plot(pop~year, pch=15)
```



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Expressions, Objects, and Methods

- ▶ Standard interaction mode in R is as follows:
 - ▶ Users enter an expression, which is evaluated by the R system. Result is printed on the screen
- ► Expressions work on *objects*
- Each object has a *class* attribute, which is a character vector
- > x <- 10
- > class(x)

[1] "numeric"

```
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```

R. sessions

The working directory.

```
> getwd()
```

[1] "C:/Users/bartz/Documents/workspace/SvnSpot.d/trunk/publications/Gecco2012Tuto

Use 1s to list contents of R's workspace:

```
> ls()
```

```
[1] "iris" "mygd" "pop" "year"
```

Quitting: Note, q() is a function and can be used if R should be quit.

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Logical Operators and Vectors in R

- ▶ R implements the following logical operators
 - ▶ & , the logical "and",
 - ▶ | , the logical "or", and
 - ▶ !, the logical "not" operator
- ▶ R commands to generate vectors:
 - ▶ c() ("concatenate"),
 - ▶ seq() ("sequence"), and
 - rep() ("replicate")
- ▶ Modes: logical, numeric, character, or list

```
> x \leftarrow c(1,2)
```

- > y <- c(3,4)
- $> z \leftarrow c(x,y)$
- > x ==y
- [1] FALSE FALSE

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Vectors in R.

- ▶ R's repeat command rep() can be used in two variants
 - ▶ To repeat the numerical value one ten times, we use

```
> rep(1,10)
[1] 1 1 1 1 1 1 1 1 1 1
```

▶ The second argument to the rep() command can be a vector.

```
> v <- c(1,2,4)
> letters <- c("a","b","c")
> rep(letters, v)
[1] "a" "b" "b" "c" "c" "c" "c" "c"
```

► Here, the first element "a" is repeated once, the second element "b" twice, and the third element "c" four times

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Calculations with Vectors in R

Calculations with vectors of the same length (like ordinary numbers)

```
> x <- c(1,2,3)
> y <- c(1,2,4)
> x+y
```

[1] 2 4 7

▶ Relational expressions can be evaluated as follows

> x < y

[1] FALSE FALSE TRUE

▶ If vectors do not have the same length, the shorter vector is recycled

```
> y <- c(5,6)
> x+y
[1] 6 8 8
```

▶ Vector v modified to (5,6,5), i.e., the first element is added at the end. Both vectors have the same size and can be added

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Vectors in R: Sequences

> seq(from=5, to=22, by=3)

[1] 5 8 11 14 17 20

Short form

> seq(5,22,3)

[1] 5 8 11 14 17 20

Default step size is one. Short form with colon

> seq(0,10) == 0:10

Character vectors: vectors of text strings, entries are specified in quotes

> c("one","two","three")

[1] "one" "two" "three"

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Calculating the mean of vectors in R

Consider the vector

> x<- c(2,3,5,7)

To calculate its mean,

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i,$$

we can proceed as follows:

> sum(x)/length(x)

[1] 4.25

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Calculating the standard deviation of vectors in R

To calculate its standard deviation.

$$\mathrm{sd}(x) = \sqrt{\sum_{i=1}^n \frac{(x_i - \overline{x})^2}{n-1}},$$

we can proceed as follows:

```
> xbar <- sum(x)/length(x)</pre>
> sqrt( sum( (x - xbar)^2 / (length(x)-1) ) )
[1] 2.217356
```

Alternatively, we can use the build-in commands

> mean(x)

[1] 4.25

> sd(x)

[1] 2.217356

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Conditional Selection

▶ To modify elements of an vector, we can use the assignment operator

```
> v[1] <- -10
> v
 [1] -10 20 30 40 50 60 70 80 90 100
```

Conditional selection can be performed as follows

```
> v>50
```

[1] FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE > v[v>50]

```
[1] 60 70 80 90 100
```

- ▶ Logical operators can be used to combine several subset selection conditions.
- ▶ For example, to select entries, which are larger than 55 and smaller than 79, we can use the following command

```
> v[ v > 55 & v < 79]
[1] 60 70
```

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Subsets, and Indexing

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Brackets are used to access certain elements of a vector. To select the i-th entry of the vector v, e.g., the third entry v_3 , we can use the command

```
> v \leftarrow c(10,20,30,40,50,60,70,80,90,100)
> v[3]
[1] 30
```

This procedure is referred to as *indexing* in the following. To select a subset, we can index with a vector.

```
> v[c(3,4,5)]
[1] 30 40 50
```

Use negative subscripts to omit elements in nominated subscript positions > v[-c(2,3)]

```
[1] 10 40 50 60 70 80 90 100
```

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Missing Values. The Symbol NA

```
> y <- c(1, NA, 3, 0, NA)
[1] 1 NA 3 O NA
```

Any operation that involves NA generates NA. The following does not work as expected, all values remain unchanged:

```
> y[y==NA] <- 0
> print(y)
[1] 1 NA 3 O NA
```

To replace NA by 0, use is.na():

```
> v[is.na(v)] <- 0</pre>
> print(y)
[1] 1 0 3 0 0
```

Some functions, e.g., mean() take the argument "na.rm=T".

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Factors

Categorical data such as gender can be "female" or "male", respectively. Categorical data should be specified as factors.

```
> gender <- c(rep("female", 3), rep("male", 5))</pre>
```

To generate a factor, use R's factor() command

```
> gender <- factor(gender)</pre>
```

Now: internally 3 1s are followed by 5 2s. We can use the function as.numeric() to extract the numerical coding as numbers "1" and "2".

> gender

```
[1] female female female male male male male Levels: female male
```

```
> as.numeric(gender)
```

```
[1] 1 1 1 2 2 2 2 2
```

A factor has set of levels. "female" and "male" are the levels of the factor gender:

```
> levels(gender)
```

```
[1] "female" "male"
```

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```
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```

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Matrices and Arrays

E 17 18 19 20

To fill the matrix rowwise, we can use the argument byrow=T. To label the rows of a matrix, we can use the command rownames().

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Matrices and Arrays

Matrices and arrays are vectors with dimensions.

```
> x <- 1:20
> dim(x) <- c(5,4)
> x
     [,1] [,2] [,3] [,4]
[1,]
                 11
[2,]
[3,]
                 13
[4,]
             9
                 14
                      19
ſ5.1
            10
                 15
```

We can also use the matrix() command.

```
> matrix(1:20, nrow= 5)
     [,1] [,2] [,3] [,4]
[1,]
[2,]
[3,]
             8
                 13
                      18
[4,]
             9
                14
                      19
[5,]
            10
                 15
                      20
```

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Combining Matrices and Vectors

cbind() and rbind() combine objects such as matrices or vectors columnwise or rowwise, respectively

```
> A <- matrix(1:4, nrow= 2, byrow=T)</pre>
> B <- matrix(10*(1:4), nrow= 2, byrow=T)
> cbind(A,B)
     [,1] [,2] [,3] [,4]
[1,] 1
             2 10
> rbind(A,B)
     [,1] [,2]
[1,]
      1
[2,]
       3
[3,] 10
            20
[4.]
      30
            40
```

```
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```

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Lists

Many R functions return results as a list. Flexible structures to store heterogeneous data, e.g., numerical or boolean values.

```
> 1 <- list( c("a", "b", "c"), 1:4, c(TRUE, TRUE, FALSE))
> 1
[[1]]
[1] "a" "b" "c"
[[2]]
[1] 1 2 3 4
[[3]]
[1] TRUE TRUE FALSE
```

List 1 has three elements: 1) three strings, 2) numbers from one to four, and 3) three boolean values.

```
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```

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Adding and Deleting List Elements

List elements can be deleted by setting their values to NULL

```
> 1
[[1]]
[1] "a" "b" "c"
[[2]]
[1] 1 2 3 4
[[3]]
[1] TRUE TRUE FALSE
```

Delete the first element

```
> 1[[1]] <- NULL
> 1
[[1]]
[1] 1 2 3 4
[[2]]
[1] TRUE TRUE FALSE
```

To delete multiple list elements, we can use the minus sign

```
> 1 <- c(1,1)
> 1 <- 1[-c(3,4)]
> 1
[[1]]
[1] 1 2 3 4
[[2]]
[1] TRUE TRUE FALSE
```

```
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```

Single square brackets return a list.

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Addressing Lists

```
> 1[1]
[[1]]
[1] "a" "b" "c"
Here, 1[1] returns a list of length one, whereas 1[2:3] returns a list of
length two.
> 1[2:3]
[[1]]
[1] 1 2 3 4
[[2]]
[1] TRUE TRUE FALSE
```

List elements can be addressed by double square brackets

```
> 1[[1]]
[1] "a" "b" "c"
> 1[[1]][2]
[1] "b"
```

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Length of Lists

```
length() to determine the length of a list
> length(1)
[1] 2
Adding a new element at the end using length()
> 1[[length(1)+1]] <- c("x","y")
> 1
[[1]]
[1] 1 2 3 4
[[2]]
[1] TRUE TRUE FALSE
[[3]]
[1] "x" "y"
```

```
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```

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Naming List Elements

We can use the names() function to add names to list elements.

```
> names(1) <- c("numbers", "booleans")
> 1

$numbers
[1] 1 2 3 4

$booleans
[1] TRUE TRUE FALSE

$<NA>
[1] "x" "y"
```

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Implicit Loops Using Apply

- ▶ apply(x, margin, fun) returns a vector or array or list of values obtained by applying a function to margins of an array or matrix
- ► Margin: vector giving the subscripts which the function will be applied over
- ► For example, for a matrix 1 indicates rows, 2 columns, c(1, 2) rows and columns, or in matrices named dimnames
- ► Implicit Loops Using sapply(), lapply(), and tapply()
 - sapply() returns a simplified result (vector or matrix),
 - ► lapply() returns a list, and
 - ► tapply() creates a table

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Data Frames

Data frames can be used for grouping data. A data frame is a list of vectors of the same length.

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Implicit Loops Using lapply()

List of car data:

```
> cars <- list(speed=c(180, 250, 300),
+ price = c(10.5, 55.6, 76.0),
+ consumption=c(5, 7.1, 12.5))
> cars

$speed
[1] 180 250 300

$price
[1] 10.5 55.6 76.0

$consumption
[1] 5.0 7.1 12.5
```

Consider the sum() function.

> lapply(cars, sum)
\$speed
[1] 730

\$price
[1] 142.1
\$consumption
[1] 24.6

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Implicit Loops Using Anonymous Functions

```
An anonymous function can be used as well
```

```
> lapply(cars, function(x) return(x[2]))
$speed
[1] 250

$price
[1] 55.6

$consumption
[1] 7.1
```

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Sorting

We can use the sort() function to sort a vector.

```
> sort(iris$Sepal.Length)[1:10]
[1] 4.3 4.4 4.4 4.4 4.5 4.6 4.6 4.6 4.6 4.7
```

The order() function generates a vector of the indices of the sorted values.

```
> a <- c(20,-1,4,3)
> order(a)
[1] 2 4 3 1
```

Here, the smallest value "1" is at position 2, the next at position 4, whereas the largest value is at position 1.

```
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```

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sapply()

Given a list structure x, the function unlist() simplifies it to produce a vector. In order to obtain a vector of mean values instead of a list using the lapply() function, the following command can be used.

```
> unlist(lapply(cars, mean))
      speed      price consumption
      243.33333     47.36667     8.20000
```

Using sapply(), the same result can be obtained directly.

For example, to apply mean() to each of the iris data set columns:

```
> sapply(iris, mean)
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
    5.843333    3.057333    3.758000    1.199333    NA
```

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Sorting Using order()

```
> a
[1] 20 -1  4  3
> i <- order(a)
> i
[1] 2 4 3 1
> a[i]
[1] -1  3  4 20
```

Sorting a set of variables according to the values of some other variables:

```
> i <- order(iris$Sepal.Length)
> options(width=70)
> iris[i,][1:4,]
```

```
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
14
           4.3
                       3.0
                                    1.1
                                                0.1 setosa
9
           4.4
                       2.9
                                    1.4
                                                0.2 setosa
39
            4.4
                       3.0
                                    1.3
                                                0.2 setosa
43
            4.4
                       3.2
                                    1.3
                                                0.2 setosa
```

R Programming

Simple Formulas

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Loops with for() and while()

Loops can be generated with the for() function as follows.

```
> for( i in 1:5) print(i)
```

[1] 1

[1] 2

[1] 3

[1] 4

[1] 5

We can also use the while() command.

```
> x<-1
```

> while(x <= 5){

+ print(x)

+ x <- x+1

+ }

Γ1 1

[1] 2

[1] 3

[1] 4

[1] 5

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R Programming

Control Structures

Try using functions from the apply(x) family instead of loops. system.time() returns CPU (and other) times used by process. First, an implementation without loops.

```
> require(stats)
> x <- 1:1000000
> system.time(y <- x^2)

    user    system elapsed
    0.03    0.00    0.03</pre>
```

Next, the for() function to perform calculation with loops.

```
> x <- 1:1000000
> system.time(
+ for( i in 1:length(x)) y[i] <- x[i]^2
+ )

    user system elapsed
    2.58    0.01    2.59</pre>
```

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Loops with repeat()

Alternatively, the repeat() command can be used in combination with the break() command.

```
> x <- 1
> repeat{
+ print(x)
+ x<-x+1
+ if (x > 5) break
+ }

[1] 1
[1] 2
[1] 3
[1] 4
[1] 5
```

□ R Programming

R Functions and Arguments

R has many pre-defined functions, e.g., mean, sum, or range.

```
> year <- c(1800,1850,1900,1950,2000)
> pop <- c(18,54,500,1701,7731)
> range(year)
[1] 1800 2000
```

> summary(year)

```
Min. 1st Qu. Median Mean 3rd Qu. Max.
1800 1850 1900 1900 1950 2000
```

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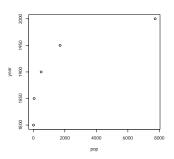
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R Basics and Technical Details

R Programming

Named Actual Arguments

- Positional matching: very simple concept, becomes unhandily if many arguments occur
- ▶ R can handle *named actual arguments*, i.e., names are matched against their formal arguments
- ▶ Output from plot() with x and y values exchanged:
- > plot(y=year, x=pop)



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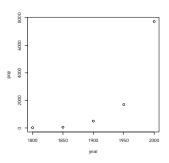
R Basics and Technical Details

R Programming

Arguments and Positional Matching

R uses positional matching, i.e., the n-th argument corresponds to the n-th function variable. For example, plot() assumes: 1st argument (year) corresponds to x, whereas 2nd (population) corresponds y

```
> plot(year, pop)
```



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R Basics and Technical Details

☐R Programming

Writing R Functions

Using R's function() function, we can write our own functions. Note, %*% denotes matrix multiplication

```
> norm <- function(x) sqrt(x%*%x)
> norm(1:4)
```

> HOIM(1:4)

[,1] [1,] 5.477226

Curly braces can be used to define the body of the function.

```
> h <- function(x){
+ if (x<0) -1</pre>
```

+ if (x<0) -+ else 1}

> h(1)

[1] 1

Note, we can use the command ifelse() as well.

```
> heaviside <- function(x) ifelse(x<0,-1,1)</pre>
```

> heaviside(1)

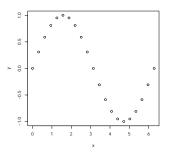
[1] 1

Graphics: The Basic Plot Command plot(x,y)

- ► The basic plot command is plot(x,y)
- ightharpoonup Alternatively, plot(y \sim x) can be used

```
> x <- (0:20)*pi/10
> y <- sin(x)
```

> plot(y~x)



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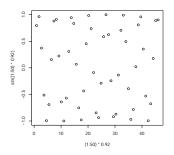
R Basics and Technical Details

└─ Graphics

Modifying the Layout

▶ par() modifies layouts, e.g., margin sizes, line widths and types, colors, clipping, character sizes and fonts

```
> plot( (1:50)*0.92, sin( (1:50)*0.92))
```



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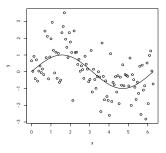
R Basics and Technical Details

☐ Graphics

Combining Plots

▶ Add lines to this plot using the function lines()

```
> n<-100
> x <- (0:n)*2*pi/100
> y <- sin(x)+rnorm(n+1)
> plot(y~x)
> lines(x,sin(x))
```



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R Basics and Technical Details
Graphics

Modifying the Layout

Now we plot the same figure again with a modified layout. In addition, two new figures are plotted

R Basics and Technical Details

Importing and Exporting Data

Importing from Text Files

- read.table() is an easy to use method to importing data from a simple text file
- ► Simple test file, say "simple.txt":

```
1 2
2 4
3 6
```

4 8

> df.simple <- read.table("simple.txt", header = TRUE)
> df.simple

ху

1 1 2 2 2 4

3 3 6

4 4 8

▶ The result of the read.table() is a data frame.

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Exploratory Data Analysis

Exploratory data analysis (EDA): Overview

- ▶ Idea: let the data speak for themselves
- ▶ Use of human brain's abilities as a pattern recognition device
- ► Reveal new information ("playing trumpet to the tulips")
- ▶ Ways how explore data prior to a formal analysis
- ► Standard tools:
 - ► Histograms and density plots
 - Stem-and-leaf plots
 - Scatter plots
 - ► Lattice: lowess smoother, trellis graphics
- ► Histograms: graphical representations of the frequency distribution of sets of data
- ► Areas of the plotted rectangles proportional to the number of observations with values within rectangle width
- ▶ Add density curves, they do not rely on breakpoints

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R Basics and Technical Details

Importing and Exporting Data

Exporting to Text Files

- ▶ write.table() prints its required argument x (after converting it to a data frame if it is not one nor a matrix) to a file or connection
- write.csv() and write.csv2() provide convenience wrappers for writing CSV files

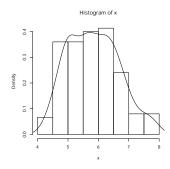
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Exploratory Data Analysis

Histograms and Density Plots

- > data(iris)
 > x <- iris\$Sepal.Length</pre>
- > dens <- density(x)
- > hist(x,freq=F)
- > lines(dens)



Exploratory Data Analysis

Stem-and-leaf plots

- ▶ The stem is on the left, leaves are on the right
- ▶ Smallest value reads 42. The value 44 appears four times
- > stem(iris\$Sepal.Length)

```
The decimal point is 1 digit(s) to the left of the |
```

```
42 | 0

44 | 0000

46 | 000000

48 | 00000000000

50 | 0000000000000000

52 | 00000

54 | 0000000000000
```

58 | 0000000000

60 | 00000000000

62 | 0000000000000

64 | 00000000000 66 | 000000000

68 | 0000000

70 | 00

72 | 0000

76 | 00000

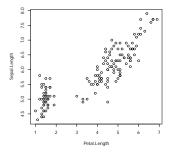
70 | 00

78 | 0

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Scatterplots

- ▶ Simple but effective tool for the analysis of pairwise relationships
- > plot(Sepal.Length~Petal.Length,data=iris)

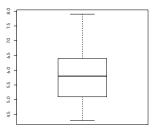


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Exploratory Data Analysis

Boxplots

- ▶ Boxplots summarize graphically the following information:
 - Outliers
 - ► Smallest and largest value (outliers excluded)
 - ► Lower and upper quantile
 - Median
- > boxplot(iris\$Sepal.Length)



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What to Look for in Plots: Outliers

- ► Points that appear to be isolated from the main region of the data are called outliers
- Outliers can distort models to be fit to the data
- ▶ But there is no general definition for outliers
- ▶ This definition depends on our view of the data
- ► Boxplots are useful to detect outliers in one dimension, scatterplots are useful in two dimensions
- ► However, sometimes outliers will be apparent only in three or more dimensions.

Exploratory Data Analysis

Exploratory Data Analysis

Exploratory Data Analysis

What to Look for in Plots

- Asymmetry
 - Most asymmetric distributions are positively or negatively skewed
 - Positively skewed distributions can be characterized as follows: There is a long tail to the right, values near the minimum are bunched up together, and the largest values are widely dispersed
- Different variabilities
 - Sometimes variability increases as data values increase
 - ► Then the logarithmic transformation can be helpful
- Clustering
 - ▶ Outliers can be considered as a special form of clustering
 - Clusters may suggest structures in the data which may or may not have been expected
 - Scatterplots can be useful to detect clusters.
- Non-linearity
 - Linear models should not be fitted to data where relationships are non-linear

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L Design of Experiments (DoE)

L_{Taxonomy}

A Taxonomy of Algorithm and Problem Designs

- Classify parameters
- Parameters may be qualitative, like for the presence or not of an recombination operater or numerical, like for parameters that assume real values
- ▶ Our interest: understanding the contribution of these components
- Statistically speaking: parameters are called factors
- ► The interest is in the effects of the specific *levels* chosen for these factors

Tutorial: Statistical Analysis of Optimization Algorithms with R

☐ Distributions and Random Number Generation

Distributions

Example (Binomial distribution)

► Determine five random numbers following a binomial (100, 1/5) distribution

```
> set.seed(123)
> rbinom(5, size = 100, p=1/5)
```

[1] 18 23 19 25 26

► Hundred samplings with replacement from a box with 64 black and 16 red balls. Probability of drawing a red ball is p = 16/(64 + 16) = 1/5.

- ▶ Probability that ten red balls are drawn, i.e., P(X = 10)
- > dbinom(10,100,1/5)

[1] 0.00336282

▶ CDF, i.e., compute $P(X \le 10)$

> sum(dbinom(0:10, 100, 1/5))

Γ17 0.005696381

> pbinom(10,100,1/5)

[1] 0.005696381

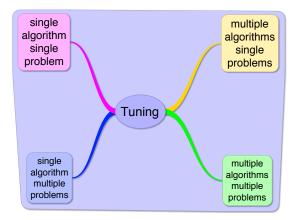
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Design of Experiments (DoE)

L_{Taxonomy}

Problems and Algorithms



- ► How to perform comparisons?
- ► Adequate statistics and models?

Taxonomy

SASP: Algorithm and Problem Designs

- ightharpoonup Basic design: assess the performance of an *optimization algorithm* on a single problem instance π
- ► Randomized optimization algorithms ⇒ performance *Y* on one instance is a random variable
- ▶ Experiment: On an instance π algorithm is run r times \Rightarrow collect sample data Y_1, \ldots, Y_r (independent, identically distributed)
- One instance π , run the algorithm r times $\Rightarrow r$ replicates of the performance measure Y, denoted by Y_1, \ldots, Y_r
- ► Samples are conditionally on the sampled instance and given the random nature of the algorithm, independent and identically distributed (i.i.d.), i.e.,

$$p(y_1, ..., y_r | \pi) = \prod_{j=1}^r p(y_j | \pi).$$
 (1)

• Y might be described by a probability density/mass function $p(y|\pi)$

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Tutorial: Statistical Analysis of Optimization Algorithms with R $\$ Design of Experiments (DoE) $\$ $\$ $\$ $\$ $\$ $\$ Taxonomy

SAMP: Algorithm and Problem Designs

- ► Multiple problem instances occur if optimization problems have a set of input data which instantiate the problem
- ▶ Experiment: collect sample data $Y_1, ..., Y_R$ (independent, identically distributed)
- Goal: Drawing conclusions about a certain class or population of instances Π
- ightharpoonup Single algorithm, multiple problems: performance Y of the algorithm on the class Π is described by the probability function

$$p(y) = \sum_{\pi \in \Pi} p(y|\pi)p(\pi), \tag{2}$$

with $p(\pi)$ being the probability of sampling instance π

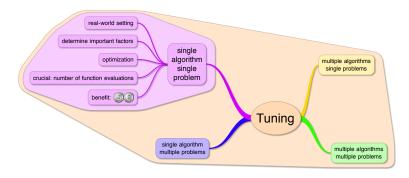
▶ In other terms, we are interested in the distribution of *Y* marginalized over the population of instances

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Design of Experiments (DoE)

∟_{Taxonomy}

SASP - Single Algorithm, Single Problem



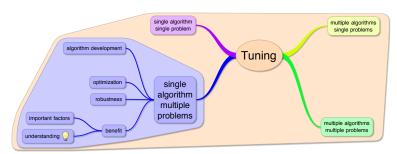
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L Design of Experiments (DoE)

└─ Taxonomy

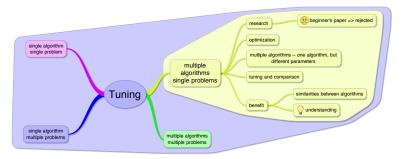
SAMP - Single Algorithm, Multiple Problems



Design of Experiments (DoE) L_{Taxonomy}

MASP: Algorithm and Problem Designs

- Several optimization algorithms are compared on one fixed problem instance π
- \triangleright Experiment: collect sample data Y_1, \ldots, Y_R (independent, identically distributed)
- ▶ Goal: comparison of algorithms on one (real-world) problem instance



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Design of Experiments (DoE)

L Taxonomy

MAMP: Randomized Problem Designs

- ▶ Sometimes, several hundred (or even more) problem instances to be tested ⇒ interest not just on the performance of the algorithms on a few specific instances, but rather on the generalization of the results to the entire population of instances
- ▶ Procedure: instances are chosen at random from a large set of possible instances of the problem
- ▶ Statistically, instances are also levels of a factor
- ▶ However, factor is of a different nature from the fixed algorithmic factors described above
- ▶ Levels are chosen at random and the interest is not in these specific levels but in the population from which they are sampled
- ▶ ⇒ levels and the factor are random
- ▶ This leads naturally to a mixed model [4]

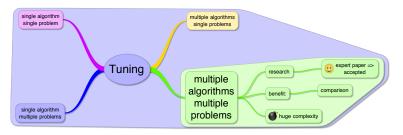
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Design of Experiments (DoE)

L_{Taxonomy}

MAMP: Fixed Algorithm and Problem Designs

- ► Typically:
 - ▶ Take a few, fixed instances for the problem at hand
 - ► Collect the results of some runs of the algorithms on these instances
- ▶ Statistically, instances are also levels of a factor
- Instances treated as blocks
- ▶ All algorithms are run on each single instance
- ▶ Results are therefore *grouped* per instance



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Design of Experiments (DoE) L_{Taxonomy}

MAMP: Randomized Problem Designs

- Organize our presentation in different cases according to the number and type of factors involved
- ▶ Identify the cases with the following notation:

```
algorithm number of instance factors factors factors
                                                   number of
```

- ▶ Lower-case letters when referring to the number of factors, upper-case letters when referring to the number of levels
- ▶ Dash (-) indicates absence of fixed factors, round parenthesis indicates nesting
- **Example:** $\langle N, q(M), r \rangle$ means N algorithmic factors, q instances sampled from each combination of M instance factors, and r runs of the algorithm per instance

∟_{Taxonomy}

MAMP: Nested Linear Mixed Models

- ▶ In statistics, the effects described are modeled as linear combinations, and mathematical theory has been developed to make inferences about the populations on the basis of the results observed in the samples.
- ► The mixed nature of the factors leads to so-called *nested linear* mixed models
- Nontrivial designs, go beyond the classical multifactorial ANOVA, where all factors are instead treated as fixed
- Mathematical formula involved and the inference derived are different in the case of mixed-effects models and this may lead to a different inference
- ▶ [4] give an example where this difference clearly arises

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L Design of Experiments (DoE)

Algorithm and Problem Designs

- ► Classify parameters
 - ► Continuous, categorical, etc.
- Designs

L Taxonomy

- ► Factorial, fractional factorial, space filling, etc.
- Models
 - ► ANOVA, regression, kriging, tree-based models, etc.
- R packages for experimental designs: Groemping's CRAN Task View: Design of Experiments (DoE) & Analysis of Experimental Data http:

//cran.r-project.org/web/views/ExperimentalDesign.html

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L Design of Experiments (DoE)
L Taxonomy

Summary: A Taxonomy of Algorithm and Problem Designs

- ► Taxonomy combining ideas from [1] and [4]
- Experimental design notation:

```
\left\langle \begin{array}{c} \text{algorithm} & \text{number of} \\ \text{factors} \end{array} \right\rangle , \begin{array}{c} \text{number of} \\ \text{instances} \end{array} \left\langle \begin{array}{c} \text{instance} \\ \text{factors} \end{array} \right\rangle , \begin{array}{c} \text{number of} \\ \text{runs} \end{array} \right\rangle .
```

- ▶ Case $\langle -, q(-), r \rangle$: Random-Effects Design: one algorithm is evaluated on q instances randomly sampled from a class Π
- ► Case $\langle N, q(-), r \rangle$: Mixed-Effects Design: *h algorithms* are evaluated on *q instances* randomly sampled from a class Π
- ▶ Case $\langle 1,1(1),r\rangle$: Fixed-Effects Design: one algorithm is evaluated r times on one fixed instance π

. . . .

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Design of Experiments (DoE)

Taxonomy

Comparison of Two Simulated Annealing Parameter Settings

▶ Case (2,1(1),r): Fixed-Effects Design: one *algorithm* is evaluated on one *instance* π (fixed), i.e., SASP

```
> set.seed(123)
> library(SPOT)
> fn <- spotBraninFunction #test function to be optimized by SANN
> x0 <- c(-2,3) #starting point that SANN uses when optimizing Branin
> maxit <- 100 #number of evaluations of Branin allowed for SANN
> temp <- 10
> tmax <- 10
> n <- 100
> v <- rep(1.n)
> y0<-sapply(y, function(x) x<-optim(par=x0, fn=fn, method="SANN"
                                     , control=list(maxit=maxit,
                                                     temp=temp, tmax=tmax))$value)
> temp <- 4
> tmax <- 62
> y <- rep(1,n)
> y1<-sapply(y, function(x) x<-optim(par=x0, fn=fn, method="SANN"
                                      , control=list(maxit=maxit,
                                                     temp=temp, tmax=tmax))$value)
```

Design of Experiments (DoE)

∟_{Taxonomy}

Comparison: Simple EDA Using Boxplots

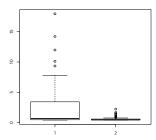
```
> summary(y0)
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 0.3984 0.4444 0.6587 2.2770 3.4020 17.9600
```

> summary(y1)

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 0.3985 0.4150 0.4439 0.5609 0.5736 2.2250
```

> boxplot(y0,y1)



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L_Design of Experiments (DoE)

Taxonomy

Simple EDA: Let the Data Speak

- > df1 <- read.table("Data.d/NULL.res",header=T)</pre>
- > options(width=80)
- > df1[1:10,]

	Function	XDIM	YDIM	STEP	SEED	CONFIG	VARX1	VARX2	Y
1	UserSuppliedFunction	2	1	0	1234	1	23	62	0.5183426
2	UserSuppliedFunction	2	1	0	1235	1	23	62	0.4020790
3	UserSuppliedFunction	2	1	0	1234	2	62	33	3.5002149
4	UserSuppliedFunction	2	1	0	1235	2	62	33	16.6525805
5	UserSuppliedFunction	2	1	0	1234	3	38	26	4.7735424
6	UserSuppliedFunction	2	1	0	1235	3	38	26	0.3987177
7	UserSuppliedFunction	2	1	0	1234	4	70	16	1.4725001
8	UserSuppliedFunction	2	1	0	1235	4	70	16	18.1272253
9	UserSuppliedFunction	2	1	0	1234	5	8	90	0.5871467
10	UserSuppliedFunction	2	1	0	1235	5	8	90	0.6200017

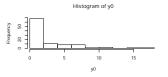
```
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```

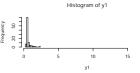
Design of Experiments (DoE)

L_{Taxonomy}

Comparison: Simple EDA Using Histograms

```
> par(mfrow=c(2,1))
> hist(y0,xlim = c( min(y0,y1), max(y0,y1)))
> hist(y1,xlim = c( min(y0,y1), max(y0,y1)))
> par(mfrow=c(1,1))
```





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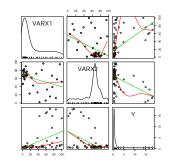
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L_Design of Experiments (DoE)

Taxonomy

Analysis: Simple EDA Using Scatterplots

- library(car)
- > scatterplotMatrix(~VARX1+VARX2+Y, reg.line=lm, smooth=TRUE,
- + spread=FALSE, span=0.5, diagonal = 'density', data=df1)



Sequential Parameter Optimization SPO

Use statistical techniques and methods from design of experiment to solve optimization problems.

- 1. Take initial samples from design space and evaluate on target function/algorithm
- 2. Build surrogate model (Linear, Tree-based, Kriging, ...) based on known evaluations
- 3. Determine promising new solutions with model
- 4. Evaluate new solutions
- 5. If termination criterion not reached: go to 2.
- 6. Summarize Results / Create Report

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R-based automated analysis and tuning, e.g., sequential parameter optimization

SPOT: Installation, Help, Demos

- ► Install from CRAN:
 - > install.packages("SPOT")
- Load package to Workspace:
- > require("SPOT")
- ► Get help on some spot functions
 - > ?spot
 - > ?spotOptim
- ► Get a list of SPOT demos
 - > demo(package="SPOT")
- ▶ Run a SPOT demo
 - > demo("spotDemo18ForresterOptim",ask=F)
- Start the GUI
 - > spotGui()

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R-based automated analysis and tuning, e.g., sequential parameter optimization

SPO Toolbox (SPOT)

- ► Currently maintained and developed as an R-Package
- ▶ Interfaces to several other R-packages
- ▶ Provides Demos and Documentation
- ► Graphical User Interface
- ▶ Alternative version is available for matlab





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R-based automated analysis and tuning, e.g., sequential parameter optimization

Applications: algorithms tuned by SPOT

- Several types of evolution strategies
- ▶ Time series prediction and anomaly detection
- Classification
- ► Symbolic Regression
- Simulated Annealing
- ► For more applications see [2]

R-based automated analysis and tuning, e.g., sequential parameter optimization
SPOT Demo

Simulated Annealing SANN

- Randomized optimization algorithm
- ► Two parameters: starting temperature TEMP and number of function evaluations at each temperature TMAX
- ▶ implementation used: optim, part of R-base

```
> #Find minimum of 2D-sphere function with SANN
> fn<-function(x){return(sum(x^2))}
> result<-optim(par=c(2,-4),fn,method="SANN")
> result$value
[1] 0.0002277956
> result$par
[1] 0.006771081 0.013488814
```

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R-based automated analysis and tuning, e.g., sequential parameter optimization SPOT Demo

SANN sweep

- ▶ Since this is a simple test problem: Complete sweep
- ▶ Understand underlying fitness shape
- ▶ 1000 repeats for each setting (takes rather long)

```
> target <- function(x,y,x0,fn,maxit){
+ zz<-matrix(0,length(x))
+ repeats=1000
+ for(i in 1:repeats){
+ set.seed(i)
+ zz =zz + apply(cbind(x,y),1,testalgorithm,x0=x0,fn=fn,maxit=maxit)
+ }
+ return(zz/repeats)
+ }
> x <- seq(1, 100, length.out = 100)
> y <- x
> z <- outer(x, y, target,x0=x0,fn=fn,maxit=maxit)
> filled.contour(x, y, z, color.palette=heat.colors,xlab="temp",ylab="tmax")
> pal <- topo.colors(100)
> require(rg1)
> persp3d(x,y,z,col=pal[cut(z,100)],xlab="TEMP",ylab="TMAX")
```

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Tuning SANN: Define Problem to solve

► Target function: Branin-Function (2-D function with three global minima)

```
> require(SPOT)
> fn <- spotBraninFunction #test function to be optimized by SANN
> x0 <- c(-2,3) #starting point that SANN uses when optimizing Branin
> maxit <- 100 #number of evaluations of Branin allowed for SANN
> testalgorithm <- function(pars,x0,fn,maxit){
+ temp<-pars[1]
+ tmax<-pars[2]
+ y <- optim(x0, fn, method="SANN",
+ control=list(maxit=maxit,
+ temp=temp, tmax=tmax))
+ return(y$value)
+ }</pre>
```

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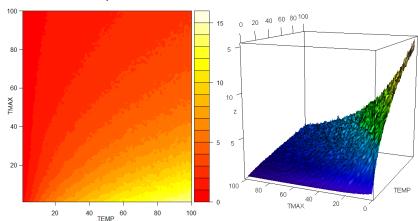
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Plots from sweep



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Tuning SANN: Configure SPOT

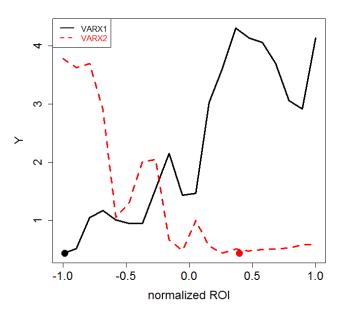
- ▶ ROI: Region of interest, in which parameters are tuned
- Surrogate: Kriging based on Forrester et. al. [6]
- Settings are minimalistic (uses a lot of default values)

```
> roi<-spotROI(c(1,1),c(100,100),type=c("INT","INT"))
> config<-list(alg.func=testalgorithm,
+ alg.roi=roi,
+ init.design.size=20,
+ seq.predictionModel.func="spotPredictForrester",
+ seq.predictionOpt.func="spotPredictOptMulti",
+ seq.predictionOpt.method="cmaes",
+ seq.predictionOpt.budget=1000,
+ report.func="spotReportSens",
+ spot.fileMode=T,
+ io.verbosity=3,
+ auto.loop.nevals=100)</pre>
```

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Tuning SANN: Run SPOT

- ▶ Pass configuration to SPOT
- ▶ Pass additional parameters to SPOT, needed by target function

```
> res<-spot(spotConfig=config,x0=x0,fn=fn,maxit=maxit)</pre>
```

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Tuning SANN: Raw results

▶ Result file, logged information separated by space

```
Function XDIM YDIM STEP SEED CONFIG VARX1 VARX2 Y UserSuppliedFunction 2 1 0 1234 1 23 62 0.518342556082896 UserSuppliedFunction 2 1 0 1235 1 23 62 0.402079045134601 UserSuppliedFunction 2 1 0 1234 2 62 33 3.50021485407806
```

Results in R command line

str(res\$alg.currentResult)

```
'data.frame': 103 obs. of 9 variables:
$ Function: Factor w/ 1 level "UserSuppliedFunction": 1 1 1 1 1 1 1 1 1 1 ...
          : num 2 2 2 2 2 2 2 2 2 2 ...
$ YDIM
          : int 1 1 1 1 1 1 1 1 1 1 ...
$ STEP
          : int 0000000000...
$ SEED
          : num 1234 1235 1234 1235 1234 ...
$ CONFIG
         : int 1122334455...
$ VARX1
          : num 23 23 62 62 38 38 70 70 8 8 ...
$ VARX2
          : num 62 62 33 33 26 26 16 16 90 90 ...
          : num 0.518 0.402 3.5 16.653 4.774 ...
```

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Tuning SANN: Other report functions

- ▶ Other reports/graphics can be created
- spotReportContour for a contour plot

```
> spot(spotConfig=append(list(
+ report.func="spotReportContour",
+ report.interactive=F),
+ res),
+ spotTask="rep")
```

spotReport3d for 3d plot

```
> spot(spotConfig=append(list(
+ report.func="spotReport3d",
+ report.interactive=F),
+ res),
+ spotTask="rep")
```

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SPOT features

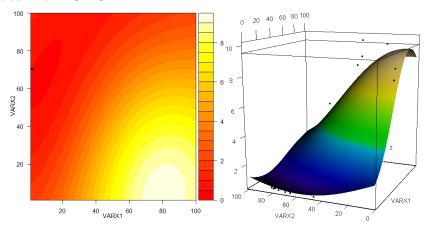
Existing features

- Single and multi criteria optimization
- ► Automated tuning, or manual steps
- ▶ modular concept: Use different combinations of models / methods
- ► Available surrogate models: Linear, Tree, Kriging, Support Vector Machine, Random Forest, ...
- ► Tuning real valued parameters as well as factors (i.e. with tree-based models)
- ▶ User can use custom models
- ▶ Different means of budget allocation
- ► Logging and Report generation

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Plots from SPOT



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Development

- Extend report functions
- ▶ Implementation of ensembles of surrogate models
- ▶ Improve multi criteria optimization
- ► Adaptive ROI
- ► New test problems or applications

R-based optimization and benchmarking resources

Overview

We will focus on:

- ► Available optimization algorithms
- Benchmarking resources

But first a very short glimpse on our targets...

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Optimization Algorithms

CRAN Task View: Optimization and Mathematical Programming http://cran.r-project.org/web/views/Optimization.html

- ▶ Huge list of available algorithms
- ▶ Also: Mathematical programming solvers
- ▶ We focus on (some) general purpose continuous solvers
- ▶ You can also deliver your implementations there (to Stefan Theussl)

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R-based optimization and benchmarking resources

The Adaptability Perspective

When adapting algorithms to a problem (or multiple), two things are of basic interest [11]:

- ► How good do we get?
- ▶ How long does it take to get there?

What to do with that?

- ▶ We can expect that different algorithms have different properties
- ► It depends on the optimization context which one is more important (algorithm selection problem)
- ▶ We encourage to further look at these aspects (together)

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Evolutionary Methods Packages

cmaes Covariance matrix adaptation evolution strategy

genalg Genetic algorithm

rgenoud GA plus quasi-Newtonian approach hybridization

pso Particle swarm optimization

DEoptim Differential evolution

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Other Interesting Methods

optim (built-in function of the stats package)
Broyden-Fletcher-Goldfarb-Shanno (BFGS) method,
bounded BFGS, conjugate gradient, Nelder-Mead, and
simulated annealing (SANN)

optimx new common frame for optim() methods and many more, e.g. bobyga, uobyga, and newuoa

nloptr supports several global optimization routines (e.g. DIRECT), local derivative-free and gradient-based (e.g. BFGS) methods used as subroutines

And many more, even interfaces to solvers (COIN-OR, CPLEX)

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BBOB Function Overview

Function groups:

- ► Separable (sphere, ellipsoidal, Rastrigin, Büche-Rastrigin, linear slope)
- ► Low or moderate conditioning (attractive sector, step ellipsoidal, Rosenbrock original, Rosenbrock rotated)
- ► High conditioning, unimodal (ellipsoidal, discus, bent cigar, sharp ridge, different powers)
- Multi-modal with global structure (Rastrigin, Weierstrass, Schaffers F7, Schaffers F7, moderately ill-conditioned, Composite Griewank-Rosenbrock F8F2)
- ► Multi-modal with weak global structure (Schwefel, Gallagher's Gaussian 101-me Peaks, Gallagher's Gaussian 21-hi Peaks, Katsuura Function, Lunacek bi-Rastrigin)

Benchmarking: BBOB

Black-Box Optimization Benchmarking (BBOB) 2012 library http://coco.gforge.inria.fr/doku.php?id=bbob-2012 (see the GECCO workshop)

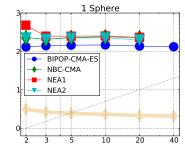
- ▶ 24 selected problems
- ▶ Interfaces from Matlab, C, Java, R, Python
- ► Lots of already existing results to compare with (BBOB 2009, BBOB 2010)
- ▶ Very powerful visualization for free (Python-based post-processing)
- ▶ You can also just use the problems

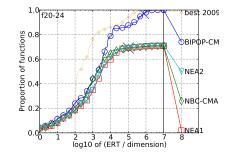
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BBOB Sample Graphics





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Real-World Problems

Noisy real-world test cases (as e.g. used in [12]) http:

//ls11-www.cs.tu-dortmund.de/rudolph/kriging/applications

Currently available:

- Gaming related: Car setup optimization (related to the former competition)
- ► Hydrogeologic Testcase: well placement
- More to come (hopefully)
- ▶ If you have other interesting problems, let us know

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Marco Chiarandini and Yuri Goegebeur.

Acknowledgments

▶ This work has been supported by the Federal Ministry of Education and Research (BMBF) under the grants FIWA (AIF FKZ 17N1009) and CIMO (FKZ 17002X11)

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